

Math 151 Quiz #2 Answers

1. (a) $\lim_{t \rightarrow 1} \frac{4t + 4}{3t^2 + 4t + 2} = \frac{8}{9}$ (We can calculate the limit by evaluating the expression at $t = 1$ since it is defined at $t = 1$.)
- (b) $\lim_{x \rightarrow -4} \frac{x^3 + 4x^2}{x^2 + x - 12} = \lim_{x \rightarrow -4} \frac{x^2}{x - 3} = -\frac{16}{7}$ (We can divide out a common factor of $x + 4$ from the numerator and denominator and then evaluate the expression at $x = -4$.)
- (c) $\lim_{n \rightarrow 3} \frac{2 + e^n}{\sqrt{\sin(\pi n) + n + 1}} = \frac{2 + e^3}{\sqrt{\sin(3\pi) + 3 + 1}} = \frac{2 + e^3}{2}$ (Evaluate the expression at $n = 3$.
Note: $\sin(3\pi) = 0$)
- (d) $\lim_{x \rightarrow 3^-} \frac{e^x}{|x - 3|} = \infty$ (Note: The limit is infinite since the numerator is approaching a non-zero number (e^3) and the denominator is approaching 0. Since the numerator is positive near $x = 3$ and the denominator is positive (absolute values are always non-negative), the limit must be $+\infty$.)
- (e) $\lim_{x \rightarrow 3^+} \frac{e^x}{|x - 3|} = \infty$ (Exact same reasoning as part (d).)

2. The function $g(x)$ is continuous at all real values except $x = 1$ or $(-\infty, 1) \cup (1, \infty)$.

Here's why:

Note that $\frac{1}{x-1}$ is discontinuous at $x = 1$ and continuous for all other values of $x > 0$, so $g(x)$ is continuous for $x > 0$ except at $x = 1$.

Also note that $x^2 - 1$ is continuous for all values $x < 0$.

The only other x -value that must be checked for continuity is $x = 0$. Note that:

- $g(0) = 0^2 - 1 = -1$.
- $\lim_{x \rightarrow 0^-} g(x) = \lim_{x \rightarrow 0^-} x^2 - 1 = -1$
 $\Rightarrow \lim_{x \rightarrow 0} g(x) = -1$
- $\lim_{x \rightarrow 0^+} g(x) = \lim_{x \rightarrow 0^+} \frac{1}{x-1} = -1$

Since $g(0) = \lim_{x \rightarrow 0} g(x)$, g is continuous at $x = 0$. (The function does **not** have a jump at $x = 0$.)