

1. Suppose  $D_{\vec{u}}f(7, 9) = 4$  for  $\vec{u} = \langle 2, 3 \rangle$ . Find the value of each of the following. If it is not possible to calculate the value say so.
  - a.  $D_{\vec{v}}f(7, 9)$  for  $\vec{v} = \langle 200, 300 \rangle$ .
  - b.  $D_{\vec{v}}f(7, 9)$  for  $\vec{v} = \langle -200, -300 \rangle$ .
  - c.  $D_{\vec{v}}f(7, 9)$  for  $\vec{v} = \langle -3, 2 \rangle$ .
  
2. Say whether each of the following statements is true or false. If false, change a couple of words in the statement to make it true.
  - a. If  $z = f(x, y)$  is a function of two variables and  $\vec{u} = \langle 6, 1 \rangle$  is a vector such that the directional derivative of  $f$  at the point  $(2, 5)$  in the direction of  $\vec{u}$  is as large as possible, then  $\nabla f(2, 5) = \langle 6, 1 \rangle$ .
  - b. If  $z = f(x, y)$  is a function of two variables, then the vector  $\nabla f(a, b)$  is perpendicular to the surface  $z = f(x, y)$  at the point  $(a, b, f(a, b))$ .
  - c. If  $w = f(x, y, z)$  is a function of three variables, then the vector  $\nabla f(a, b, c)$  is perpendicular to the surface  $f(a, b, c) = f(x, y, z)$  at the point  $(a, b, c)$ .
  
3. Suppose the temperature (in  $C^\circ$ ) at a point  $(x, y, z)$  in space is given by the function  $T(x, y, z) = 3x^2 + 2y^2 + z^2$ .
  - a. Describe the isotherms - that is, describe as precisely as possible the set of points where the temperature is constant.
  - b. In which direction from the point  $(1, 1, 1)$  does the temperature increase at the fastest rate? What is the rate of temperature increase in this direction?
  - c. Suppose a particle passes through the point  $(1, 1, 1)$  as it moves in a straight line toward the point  $(2, 1, 0)$  at the constant speed of 10 units/sec. Find the rate at which the temperature of the surrounding environment of the particle is changing at the instant it passes through the point  $(1, 1, 1)$ .
  
4. Find a parameterization of the steepest tangent line to the surface  $z = f(x, y) = \sqrt{9 - x^2 - y^2}$  at the point  $(2, 1, 2)$ .